## Exercise 74

For the following exercises, use the graphs to write a polynomial function of least degree.


## Solution

Use the labelled $x$-intercepts to write the model polynomial function.

$$
f(x)=A(x+300)^{2}(x-100)^{3}
$$

The factor $(x+300)$ is squared because the graph bounces back after hitting the $x$-axis, and the factor $(x-100)$ is cubed because locally at $x=100$ the graph is cubic. Use the labelled $y$-intercept to determine $A$.

$$
-90000=A(0+300)^{2}(0-100)^{3} \quad \rightarrow \quad-90000=A(-90000000000) \quad \rightarrow \quad A=\frac{1}{1000000}
$$

Therefore,

$$
f(x)=\frac{1}{1000000}(x+300)^{2}(x-100)^{3} .
$$

